

Hybrid: logistic veg + threshold 1/2 => classification

Sign 
$$(\underline{w}_{1}^{T}\underline{x}) = sign(\underline{\Theta}(\underline{w}_{1}^{T}\underline{x}) - \underline{1})$$

Differences?

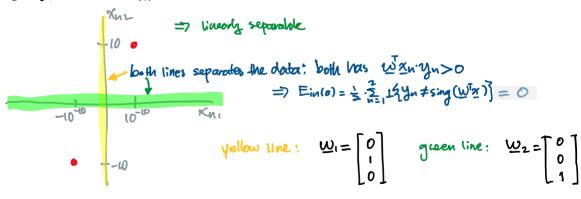
The neights would be different:  $(\underline{w}_{1}^{T} \neq \underline{w}_{2}^{T})$ 

PLA VS. Grad Des.

+1/-1 error VS. (nosk entropy error.

Ex.  $d=2$   $N=2$   $\underline{X}_{1}=(1,10^{-10},10)^{T}$   $N=1$ 
 $\underline{X}_{2}=(1,10^{-10},10)^{T}$   $N=1$ 

Linear Classification:



Lagistic Regression:  $Ein(\underline{U}) = \frac{1}{2} \sum_{n=1}^{2} log(1+e^{-tD^{-1D}})$ yellow line:  $= log(1+e^{-tD^{-1D}}) \approx 1$ green line:  $= log(1+e^{-tD^{-1D}}) \approx 1$ 

## Multidass Logistic Regression

alternative to multiclass binary classifiers:

-> Softmax or multinomial logistic regression

$$y \in \{1, 2, ..., K\}$$

$$W = \begin{bmatrix} \underline{w}_1^T \\ \underline{w}_2^T \\ \vdots \\ \underline{w}_k^T \end{bmatrix} \Rightarrow \hat{p}_w(c|\underline{x}) \simeq e^{\underline{w}_c^T\underline{x}}$$

$$\Rightarrow \hat{p}_w(c|\underline{x}) = \frac{e^{\underline{w}_c^T\underline{x}}}{\sum_{i=1}^{K} e^{\underline{w}_i^T\underline{x}}}$$

$$\begin{cases} \text{softmax classifier.} \end{cases}$$

Lass resembles CE loss: